

حلول للشيات الحيات
الطبياسية

Sheet 2: static characteristics

Prob ①:- $A_1(Q) = 101.5 \text{ L/min}$ & $A(Q) = 100.4 \text{ L/min}$

Req:- ΣA , $\Sigma C = ??$

$$\Sigma A = A_1 - A = 1.1 \text{ L/min}$$

$$\Sigma C = -\Sigma A = A - A_1 = -1.1 \text{ L/min}$$

Prob ②:- $A_1(V_1) = 109.5 \text{ Volt}$ & $A(V) = ??$ & $\Sigma A = -0.37 \text{ Volt}$
Req

$$A = A_1 - \Sigma A = 109.5 - (-0.37) = 109.87 \text{ Volt}$$

Prob ③:- $A_1(V_1) = 4.65 \text{ mls}$ & $A(V) = 4.98 \text{ mls}$

Req:- E_r ?!!

$$E_r = \frac{\Sigma A}{A} = \frac{A_1 - A}{A} = \frac{4.65 - 4.98}{4.98} = -0.066265$$

Prob ④:- $X_{\min} = 5 \text{ mmHg}$ & $X_{\max} = 760 \text{ mmHg}$ & accuracy = $\pm 1\%$

Req:- Scale Range, span, Maximum static error.

$$\text{Scale Range} = X_{\max} = 760 \text{ mmHg}$$

$$\text{Scale Span} = X_{\max} - X_{\min} = 755 \text{ mmHg}$$

static error $\left\{ \begin{array}{l} \rightarrow \text{as a ratio of Range} \\ \rightarrow \text{as a ratio of span} \end{array} \right.$ but Range \geq span

\therefore Maximum static error is to be considered as a ratio of Scale Range

$$E_s = \frac{\pm 1}{100} \times 760 = \pm 7.6 \text{ mmHg}$$

Prob 5:- $d = 0.3 \text{ mm}$ & sensitivity $= 3 \text{ mm/}^\circ\text{C}$

$$\alpha_{\text{Hg}} = 0.181 \times 10^{-3} \text{ /}^\circ\text{C}$$

Req:- bulb Volume (V) = ?? mm^3

$$\Delta V = V \alpha \Delta T = \Delta h \times A$$

$$\therefore V = \frac{\Delta h \times A}{\alpha \Delta T} = \frac{3 \times \frac{\pi}{4} \times 0.3^2}{0.181 \times 10^{-3} \times 1} = 1171.59 \text{ mm}^3$$

Prob 6:- Determine the linearity of a Potentiometer to obtain an error not to exceed 1 Part in 10000.

$$\therefore e\% = \frac{(e_l)_{\text{Max}}}{V_o} \times 100 = \frac{1}{10000} \times 100 = 0.01 \%$$

Prob 7:- An instrument requires a current of 0.05 A to overcome initial friction and produce motion of the moving parts. Define the effect and the which produce it.

Dead Zone :- هي أكبر قيمة تغير في الدخل قبل أن يبدأ الجهاز في الاستجابة ويعطى قراءة.
The effect is the Dead Zone $= 0.05 \text{ A}$

Prob 8:- Dead zone $= 0.125\%$ of span calibration: $800^\circ\text{C} \rightarrow 1800^\circ\text{C}$
what temperature change must occur before it is detected?

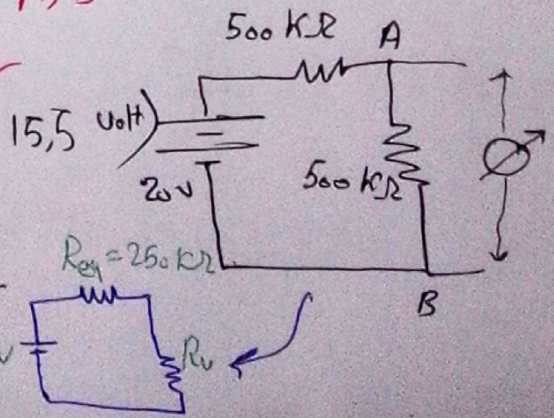
$$\text{Dead Zone} = \frac{0.125}{1000} \times (1800 - 800) = 1.25^\circ\text{C}$$

Prob 9:- Voltmeter } $= 20 \text{ k}\Omega$ 1 V
Sensitivity

Req:- what is the true value across A, B
what is the reading of voltmeter
on the following ranges: 50, 15, 5 V

$$\text{True Value} = 20 \text{ V} \left(\frac{500}{500 + 500} \right) \times 500 = 10 \text{ V}$$

Range	R_v	Reading
50	$\Rightarrow 1000 \text{ k}\Omega$	8 V
15	$\Rightarrow 300 \text{ k}\Omega$	5.45 V
5	$\Rightarrow 100 \text{ k}\Omega$	2.86 V



Prob ① Flow meter :- accuracy $\pm 0.75\%$ of scale reading
 $\hookrightarrow 0 \rightarrow 100 \text{ m}^3/\text{s}$ above 20% of scale Reading
 what is the static error if the instrument indicate $80 \text{ m}^3/\text{s}$

The static error

$$\delta Q = \pm \frac{0.75}{100} \times 100 = \pm 0.75 \text{ m}^3/\text{s}$$

Prob ② $d = 0.1 \text{ m}$ $U = 1 \text{ m/s}$ $\delta \frac{d}{d} = \pm 0.1\%$ $\frac{\delta U}{U} = \pm 3\%$

Req: (a) & (b) Range

$$Q = AV = \frac{\pi d^2}{4} U = \frac{\pi \times 0.1^2 \times 1}{4} = \frac{31.416}{4} \text{ L/s} = 7.854$$

$$\therefore \frac{\delta Q}{Q} = \left(2 \frac{\delta d}{d} + \frac{\delta U}{U} \right) = \left(2 \times \frac{1}{100} + \frac{3}{100} \right) = \pm \frac{5}{100}$$

$$= \pm 0.3927 \text{ L/s}$$

$$7.461 \leq Q \leq 8.247$$

$$\therefore \delta Q = \pm \frac{1.5708}{4} \text{ L/s}$$

$$\therefore Q \text{ Range: from } Q - \delta Q = \frac{31.416 - 1.5708}{4} = \frac{29.845}{4} \text{ L/s}$$

$$\text{to } Q + \delta Q = \frac{31.416 + 1.571}{4} = \frac{32.987}{4} \text{ L/s}$$

Prob ③ :- $R_1 = 500 \Omega \pm 1\%$, $R_2 = 615 \pm 1\%$, $R_3 = 100 \pm 0.5\%$

Req: (a) R_4 (b) δR_4 (c) $\frac{\delta R_4}{R_4}$

$$\therefore R_4 = \frac{R_1 R_2}{R_3} = \frac{500 \times 615}{100} = 3075 \Omega$$

$$\therefore \frac{\delta R_4}{R_4} = \pm \left[\frac{\delta R_1}{R_1} + \frac{\delta R_2}{R_2} + \frac{\delta R_3}{R_3} \right] = \pm \frac{2.5}{100} = \pm 2.5\%$$

$$\therefore \delta R_4 = 3075 \times \frac{2.5}{100} = 76.875 \Omega$$

Prob (4):- $R_1 = 200 \Omega \pm 5\%$, $R_2 = 100 \Omega \pm 5\%$, $R_3 = 50 \Omega \pm 5\%$

Req: R_{eq} , δR_{eq} , $\frac{\delta R_{eq}}{R_{eq}}$ → (a) if R_1, R_2, R_3 Connected in series
→ (b) Connected in Parallel

Case ①:- R_1, R_2, R_3 Connected in series

$$\therefore R_{eq} = R_1 + R_2 + R_3$$

$$= 200 + 100 + 50 = 350 \Omega$$

$$\frac{\delta R_{eq}}{R_{eq}} = \left[\frac{R_1}{R_T} \cdot \frac{\delta R_1}{R_1} + \frac{R_2}{R_T} \cdot \frac{\delta R_2}{R_2} + \frac{R_3}{R_T} \cdot \frac{\delta R_3}{R_3} \right]$$

$$= \left[\frac{200}{350} \times 0.05 + \frac{100}{350} \times 0.05 + \frac{50}{350} \times 0.05 \right] = \pm 5\%$$

$$\therefore \delta R_{eq} = 0.05 \times 350 = 17.5 \Omega$$

Case ②:- R_1, R_2, R_3 Connected Parallel

$$R_T = \frac{R_1 R_2 R_3}{R_1 R_2 + R_2 R_3 + R_1 R_3} = \frac{200 \times 100 \times 50}{300 + 150 + 250} = \frac{200}{7} \Omega$$

assume $R_1 R_2 R_3 = X$, $R_1 R_2 = a$, $R_2 R_3 = b$, $R_1 R_3 = c$, $a + b + c = Y$

$$\therefore a = 2 \times 10^4, \frac{\delta a}{a} = 10\%, \delta a = 2 \times 10^3$$

$$\therefore b = 1 \times 10^4, \frac{\delta b}{b} = 0.1, \delta b = 1 \times 10^3$$

$$\therefore c = 5 \times 10^3, \frac{\delta c}{c} = 0.1, \delta c = 500$$

$$\therefore Y = 3.5 \times 10^4, \frac{\delta Y}{Y} = \delta a + \delta b + \delta c = 3.5 \times 10^3, \frac{\delta Y}{Y} = 10\%$$

$$\therefore X = 1 \times 10^6, \frac{\delta X}{X} = \left(\frac{\delta R_1}{R_1} + \frac{\delta R_2}{R_2} + \frac{\delta R_3}{R_3} \right) = 15\%, \delta X = 15 \times 10^4$$

$$\therefore \frac{\delta R_T}{R_T} = \left(\frac{\delta X}{X} + \frac{\delta Y}{Y} \right) = 25\%$$

$$\therefore \boxed{\delta R_T = \frac{50}{7}}$$

$$\boxed{R_T = \frac{200}{7}}$$

$$\boxed{\frac{\delta R_T}{R_T} = 25\%}$$

مثال آخر

$$R_1 = 200 \pm 10 \Omega$$

$$R_2 = 100 \pm 5 \Omega$$

$$R_3 = 50 \pm 2.5 \Omega$$

$$R_T = 350 \pm 17.5 \Omega$$

$$\frac{\delta R_T}{R_T} = \frac{17.5}{350} = 5\%$$

350 is the nominal value
and 17.5 is the limiting error

Prob 5; $S = \frac{3D^2 P}{16t^2}$ (N/m^2) $\therefore D = 15 \text{ mm}$ & $t = 0.2 \text{ mm}$ &
 $P = 8 \times 10^5 \text{ N/m}^2$ &
 $\frac{\delta D}{D} = \pm 1\%$, $\frac{\delta t}{t} = 3\%$,

Req:- (S) & (δS)

$$S = \frac{3 \times (0.015)^2 \times 8 \times 10^5}{16 \times (0.2 \times 10^{-3})^2} = 843.75 \times 10^6 \text{ (N/m}^2\text{)}$$

$$\frac{\delta S}{S} = \pm \left[2 \frac{\delta D}{D} + \frac{\delta P}{P} + 2 \frac{\delta t}{t} \right] = \pm \left[\frac{2 \times 1}{100} + 0 + \frac{2 \times 3}{100} \right] = \pm 8\%$$

$$\therefore \delta S = \frac{8}{100} \times 843.75 \times 10^6 = 67.5 \times 10^6 \text{ (N/m}^2\text{)}$$

Prob 11-b $P = \frac{2\pi \times 9.81 F L R}{t \times 10^6}$, $F = 4.58 \pm 0.02 \text{ kg}$, $L = 397 \pm 1.3 \text{ mm}$
 $R = 1202 \pm 1 \text{ mm}$, $t = 60 \pm 0.5 \text{ s}$

Req:- P & δP !!

$$P = \frac{2\pi \times 9.81 \times 4.58 \times 397 \times 1202}{60 \times 10^6} = 2.2452 \text{ kW}$$

$$\frac{\delta P}{P} = \left[\frac{\delta F}{F} + \frac{\delta L}{L} + \frac{\delta R}{R} + \frac{\delta t}{t} \right]$$

$$\frac{\delta P}{2.2452} = \pm \left[\frac{0.02}{4.58} + \frac{1.3}{397} + \frac{1}{1202} + \frac{0.5}{60} \right] = \pm 0.0168$$

$$\delta P = 2.2452 \times 0.0168 = \pm 0.0377 \text{ kW} = \pm 37.7 \text{ W}$$

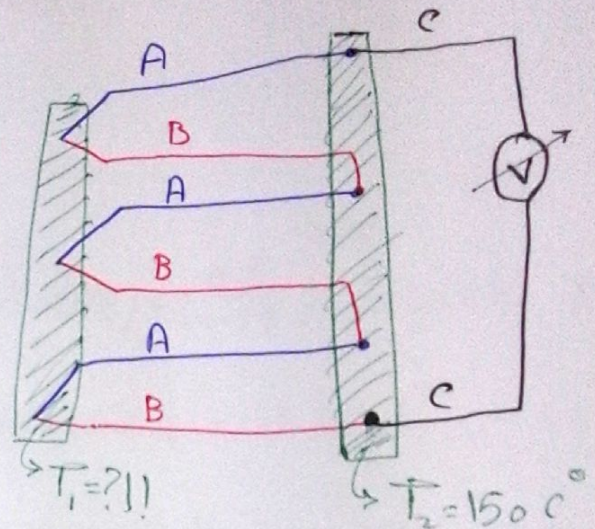
Prob 4 :- Copper - Constantan

Thermo Pile

$$T_2 = 150^\circ \text{C}$$

$$V_T = 3.3 \text{ mV}$$

Tem ($^\circ\text{C}$)	100	200	250
Volt (mV)	4.22	9.23	11.95



Req: $T_1 = ?$

$$\text{emf} = \frac{V_T}{3} + V_{(150)} = \frac{3.3}{3} + \frac{4.22 + 9.23}{2} = 7.825 \text{ mV}$$

$$T_1 = 100 + \left(\frac{9.23 - 4.22}{7.825 - 4.22} \right) \times (200 - 100)$$

$$= 100 + 100 \times \frac{3.605}{5.01}$$

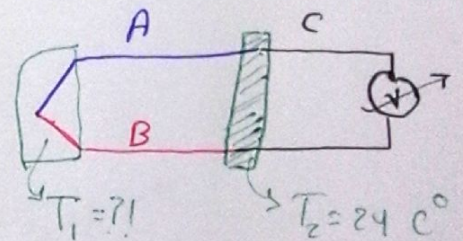
$$= 171.956^\circ \text{C}$$

100 $^\circ\text{C}$	4.22 mV
T_1 $^\circ\text{C}$	7.825 mV
200 $^\circ\text{C}$	9.23 mV

Prob 6 :- a - chromel-alumel thermocouple

$$V_T = 25.76 \text{ mV}, T_2 = 24^\circ \text{C}$$

Tem ($^\circ\text{C}$)	20	24	28	...	680	688	693
Volt (mV)	0.8	0.95	1.12	...	26.25	26.72	27.04



interpolation

$$V_{T_1} - V_{T_2} = V_{I_1} - V_{I_2}$$

$$25.76 = V_{I_1} - 0.95$$

$$V_{I_1} = 26.71 \text{ mV}$$

$$T_1 \approx 688^\circ \text{C}$$

V	T
26.25	680
26.71	T_1
26.72	688

$$T_1 = 688 - 0.01 + \frac{8}{0.47}$$

$$= 688 - \frac{8}{47}$$

$$= 687.83^\circ \text{C}$$

Prob 5A :- $T_1 = 1065^\circ\text{C}$, $\epsilon_1 = 0.82$, $\epsilon_2 = 0.75$

$$\therefore Q/A = \sigma \epsilon T_f^4$$

$$\therefore \cancel{\sigma} \epsilon_1 T_1^4 = \cancel{\sigma} \epsilon_2 T_2^4$$

$$T_2 = T_1 \times \left(\frac{\epsilon_1}{\epsilon_2}\right)^{0.25} = (1065 + 273) \times \left(\frac{0.82}{0.75}\right)^{0.25} = 1368.18 \text{ K}^\circ$$

$$\epsilon_o = T_1 - T_2 = A_1 - A = 1065 + 273 - 1368.18 = -30.18 \text{ K}^\circ$$

Prob 5 B :- $T_t = 1^\circ\text{C} = 274 \text{ K}^\circ$ / $T_w = -10^\circ\text{C} = 263 \text{ K}^\circ$ / $h = 10 \text{ W/m}^2\text{C}^\circ$

$$\epsilon_g = 0.9 \quad \text{and } \sigma = 57.2 \times 10^{-9} \text{ W/m}^2\text{K}^4$$

for steady state condition for the thermometer.

$$\textcircled{Q}_{\text{absorbed}} = \textcircled{Q}_{\text{transmitted by radiation}}$$

$$hA(T_g - T_t) = \epsilon \sigma A(T_t^4 - T_w^4)$$

$$10(T_g - 274) = 0.9 \times 57.2 \times 10^{-9}(274^4 - 263^4)$$

The glass Temperature :- $T_g = 278.4 \text{ K}^\circ = 5.4^\circ\text{C}^\circ$

then the air Temperature is 5.4°C°

Sheet 4: Pressure

Q. 1. $d_1 = 5 \text{ mm}$ & $d_2 = 150 \text{ mm}$ & $\rho_m = 13600 \text{ kg/m}^3$ &

$\Delta P = 100 \frac{\text{kN}}{\text{m}^2}$

Req: - h

$\therefore P_1 - P_2 = \rho_m g h (1 + \frac{a}{A})$

$100 \times 10^3 = 13600 \times 9.81 \times h (1 + (\frac{5}{150})^2)$

$\therefore h = 0.7487 \text{ m} = 748.7 \text{ mm}$

Prob 2 :- $d = 2 \text{ mm}$ & $D = 20 \text{ mm}$ & $(S.G.)_F = 0.8$ & $d = 5 \text{ mm}$ & $\Delta P = 1 \text{ mm Hg}$

$\therefore \Delta P = \rho_F g d (\frac{A_1}{A_2} + \sin \alpha) = \rho_w g h_w$

$S.G. = \frac{\rho_F}{\rho_w} \leftarrow 0.8 \times 5 \times 10^{-3} ((\frac{2}{20})^2 + \sin \alpha) = 1 \times 10^{-3}$

$\therefore \sin \alpha = 0.24$

$\therefore \alpha = \sin^{-1} 0.24 = 13^\circ 53' 12''$

Prob 3 :- $D = 30 \text{ mm}$ & $d = 4 \text{ mm}$ & $\Delta P = 1 \text{ mm Hg}$

Req: - $(h' - h) \rho_m$ & h & $\frac{h' - h}{h}$

$\therefore \Delta P = \rho_m g h = \rho_m g h' (1 + \frac{a}{A})$

$h = h' (1 + \frac{a}{A}) \rightarrow h' = \frac{h}{(1 + \frac{a}{A})} = \frac{1}{(1 + (\frac{1}{30})^2)} = 0.9989 \text{ m}$

$\epsilon_r = \frac{h' - h}{h} \times 100 = -0.111 \%$

$\epsilon_o = h' - h = -1.1 \text{ mm Hg} = -1.1 \times 9.81 \times 13.6 = -148.1 \text{ Pa}$

$|\epsilon_o| = 1.1 \text{ mm Hg} = 148.1 \text{ Pa}$

Prob 4 :- $D = 20 \text{ mm}$ & $d = 4 \text{ mm}$ & $d = 1 \text{ cm}$ & $\Delta P = 1 \text{ mm}$

Req:- $\alpha = ??$

$$\Delta P = \rho g d \left(\frac{a}{A} + \sin \alpha \right) = \rho g h$$

$$1 \times 10^{-2} \left(\left(\frac{4}{20} \right)^2 + \sin \alpha \right) = 1 \times 10^{-3}$$

$$\sin \alpha = 0.1 - 0.04 = 0.06$$

$$\therefore \alpha = \sin^{-1} 0.06 = 3.4398^\circ$$

Prob 5 :- $D = 30 \text{ mm}$ & $d = 5 \text{ mm}$ & $\Delta P = 1 \text{ bar}$ & $\Delta P = 1 \text{ bar}$

Req:- $h = ??$

$$\Delta P = \rho g h \left(\frac{a}{A} + 1 \right)$$

$$\therefore h = \frac{1 \times 10^5}{9.81 \times 13600 \times \left(1 + \left(\frac{5}{30} \right)^2 \right)} = 0.7293 \text{ m}$$
$$= 729.3 \text{ mm}$$

The sensitivity = $\frac{\text{out Put}}{\text{in Put}}$ \rightarrow for well manometer the out Put is h and for the U-tube manometer the out Put is h for the same in Put (ΔP)

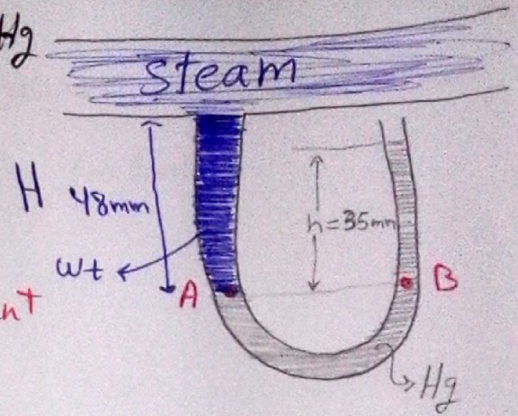
$$\text{since } h = h' \left(1 + \frac{a}{A} \right) \rightarrow h > h'$$

\therefore the sensitivity of a well manometer is less than the sensitivity of simple U-tube manometer.

Prob 62- $h = 35 \text{ mm Hg}$ & $P_{\text{atm}} = 762.1 \text{ mm Hg}$

Reqⁿ (1) $P_{\text{abs}} (\text{steam})$

(2) $\epsilon_r \%$ if Condensed water is not taken into account



$$P_A = P_B$$

$$P_{\text{Steam}} + \rho_w g H = P_{\text{atm}} + (\rho g h)_{\text{mercury}}$$

$$P_{\text{Steam}} = 9.81 \times \left((35 + 762.1) \times 10^{-3} \times 13600 - 48 \times 10^{-3} \times 1000 \right)$$
$$= 105.875 \text{ kPa}$$

$$(P_{\text{Steam}})_{\text{error}} = P_{\text{atm}} + \rho g h_{\text{(mercury)}} = 9.81 \times 797.1 \times 13.6 = 106.346 \text{ kPa}$$

$$\epsilon_{\text{error}} \% = \frac{P_{\text{error}} - P_{\text{true}}}{P_{\text{true}}} \times 100 = \frac{106.346 - 105.875}{105.875} \times 100$$

$$\epsilon_r \% = 0.44475 \%$$

Prob ① $D_i = 200 \text{ mm}$ & $d = 100 \text{ mm}$ & Venturi meter & $h = 250 \text{ mm}$
 $C_d = 0.98$ & $\rho_f = 1000 \text{ kg/m}^3$ (water)

Req: - $Q = ?$

$$Q = \frac{C_d A_1}{\sqrt{m^2 - 1}} \sqrt{2gh \left(\frac{\rho_m}{\rho_f} - 1 \right)}$$

$$= \frac{0.98 \times \pi \times 0.1^2}{\sqrt{\left(\frac{200}{100} \right)^4 - 1}} \times \sqrt{2 \times 9.81 \times 0.25 \times (13.6 - 1)}$$

$$Q = 0.13974 \text{ m}^3/\text{s} = 139.74 \text{ L/s}$$

Prob ② $\rho_{\text{oil}} = 800 \text{ kg/m}^3$ & $\rho_{\text{mercury}} = 13600$ & ρ_{air} is negligible

Req: - $E_r \%$

Case ① oil: - $\Delta P_1 = \rho g h (\rho_m - \rho_f) = g h (13600 - 800)$

Case ② air: - $\Delta P_2 = g h (\rho_m - \rho_{\text{air}}) = g h (13600)$

$$E_r \% = \frac{P_{\text{error}} - P_{\text{true}}}{P_{\text{true}}} \times 100 = \frac{g h (13600) - g h (13600 - 800)}{g h (13600 - 800)} \times 100 = \frac{800}{12800} \times 100 = 6.25 \%$$

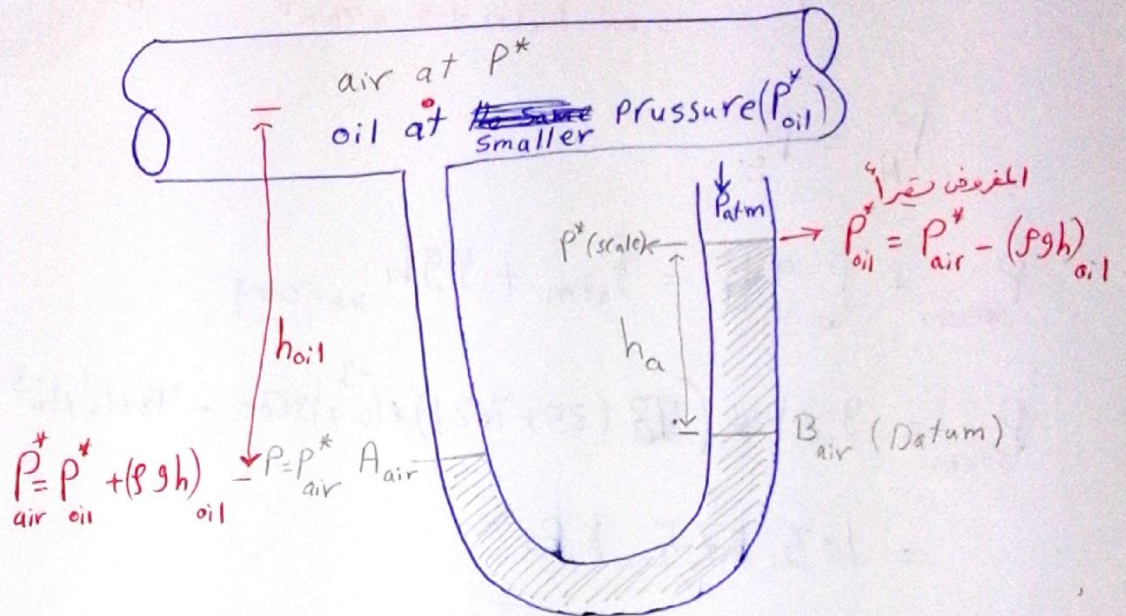
As it was originally calibrated to measure Air Pressure then the true indication will be in case of ~~water~~ ^{oil}

$$\therefore E_r \% = \frac{g h (13600 - 800) - g h (13600)}{g h (13600)} \times 100 = -5.88 \%$$

$$|E_r \%| = \frac{100}{17} \% = 5.88 \%$$

$$E_r = 6.25 \%$$

② كيفية لمساواة



$$\therefore \Delta P = P_{air}^* - P_{oil}^* = (\rho g h)_{oil}$$

Subin

$$\varepsilon_r \% = \frac{\Delta P}{P_{oil}^*} = \frac{(\rho g h)_{oil}}{P_{oil}^*} \times 100$$

$$= \frac{800 \text{ gh}}{(13600 - 800) \text{ gh}} \times 100 = 6.25 \%$$

3- $P_1 = 200 \text{ kN/m}^2$ & $T_1 = 300^\circ \text{C}$

$P_2 = 150 + 100 \text{ kN/m}^2$ & $T_2 = 200^\circ \text{C}$. $\frac{P_1 V_1}{T_1} = \text{Const}$

Req:- Correction factor = ??

$$V_1 = \frac{1}{\sqrt{m^2 - 1}} \sqrt{2gH}$$

$$Q_1 = \frac{C_d A_1}{\sqrt{m^2 - 1}} \sqrt{2gH \left(\frac{\rho_m}{\rho_f} - 1 \right)}$$

$$\rho_{f1} = \frac{P_1}{RT_1} = \frac{200 \times 10^3}{287 \times 573} = 1.216 \frac{\text{kg}}{\text{m}^3}$$

$$Q_2 = \frac{C_d A_1}{\sqrt{m^2 - 1}} \sqrt{2gH \left(\frac{\rho_m}{\rho_f} - 1 \right)}$$

$$\rho_{f2} = \frac{P_2}{RT_2} = \frac{250 \times 10^3}{287 \times 473} = 1.8416 \frac{\text{kg}}{\text{m}^3}$$

$$\therefore \text{Correction factor} = \frac{Q_2}{Q_1} = \sqrt{\frac{\left(\frac{\rho_m}{\rho_f} - 1 \right)_2}{\left(\frac{\rho_m}{\rho_f} - 1 \right)_1}} = 0.81262$$

Prob 4:- orifice ; $D = 50 \text{ mm}$ & $d = 30 \text{ mm}$ & $\rho_f = \frac{\mu d}{\gamma} = 10^5$ & $C_d = 0.61$
 $\rho = 1000 \text{ kg/m}^3$ & $\gamma = 10^{-6} \text{ m}^2/\text{s}$

Req:- V_2 orifice = ?? & $\Delta P = ??$

$$\Delta P = \rho_f g h \left(\frac{\rho_m}{\rho_f} - 1 \right)$$

$$V_1 = \frac{C_d}{\sqrt{m^2 - 1}} \sqrt{2g h \left(\frac{\rho_m}{\rho_f} - 1 \right)} = \frac{Re \gamma}{D} = \frac{10^{-6} \times 10^5}{0.05} = 2 \text{ m/s}$$

$$\Delta P = \rho_f \times g h \left(\frac{\rho_m}{\rho_f} - 1 \right) = \left(\frac{V_1^2}{C_d^2} \right) \times (m^2 - 1) \times \rho_f$$

$$\Delta P = \frac{\left(\frac{2}{0.61} \right)^2 \times \left(\left(\frac{5}{3} \right) - 1 \right)}{2} \times 1000 = 36.1 \text{ kPa}$$

$$V_2 = V_1 \times \left(\frac{D}{d} \right)^2 = m V_1 = 2 \times \frac{5}{3} = 3.33 \text{ m/s}$$

Prob 5 :- $\rho_{\text{air}} = 1.2 \text{ kg/m}^3$ & $V = 20 \text{ m/s}$ & $D = 100 \text{ mm}$ & $d = 80 \text{ mm}$

$$C_d = 0.8$$

Req: h (wt) = ?!

$$\therefore V_1 = \frac{C_d}{\sqrt{m^2 - 1}} \times \sqrt{2gh \left(\frac{\rho_w}{\rho_{\text{air}}} - 1 \right)}$$

$$20 = \frac{0.8}{\sqrt{(1.25)^2 - 1}} \times \sqrt{2 \times 9.81 \times h \left(\frac{1000}{1.2} - 1 \right)}$$

$$\therefore h = 0.0552 \text{ m} = 55.2 \text{ mm}$$

Prob 6 :- $\rho_{\text{air}} = 1.22 \text{ kg/m}^3$ & C.F. = 0.98 & $h = 80 \text{ mm}$

Req: V = ?!

$$V = \sqrt{2gh \frac{\rho_w}{\rho_{\text{air}}}} \times C.F.$$

$$= \sqrt{2 \times 9.81 \times \frac{1000}{1.22} \times 0.08} \times 0.98$$

$$V = 35.15 \text{ m/s}$$

Prob 7 :- $\Delta P = \rho gh = 100 \text{ mm wt}$ & $T = 27^\circ \text{C}$ & $P_a = 10 \text{ kN/m}^2$
 $P_{\text{atm}} = 760 \text{ mm Hg}$ & $R = 287 \text{ J/kg} \cdot \text{K}$ & S.G._{Hg} = 13.6
 C.F. = 0.98

Req: "the mean velocity"

$$\Delta P = P_b - P_a = P_b - 10 = \frac{100 \times 9.81 \times 10^3}{10^3 \times 10^3} = 0.981 \text{ kN/m}^2$$

$$\therefore P_b = 10.981 \text{ kN/m}^2$$

$$\frac{V_A^2}{2} = \left(\frac{C^2}{k-1} \right) \left[\left(\frac{P_b + P_{\text{atm}}}{P_a + P_{\text{atm}}} \right)^{\frac{k-1}{k}} - 1 \right]$$

$$\rightarrow V_A = 38.88 \times C.F. = 38.1 \text{ m/s}$$

$$P_{\text{atm}} = \frac{760 \times 9.81 \times 13.6}{10^3}$$

$$= 101.4 \text{ kN/m}^2$$

$$C = \sqrt{kRT}$$

$$= \sqrt{1.4 \times 287 \times 300}$$

$$= 347.2$$